

PDS\_VERSION\_ID = PDS3  
RECORD\_TYPE = STREAM  
RECORD\_BYTES = 80  
OBJECT = TEXT  
    PUBLICATION\_DATE = 2011-07-01  
    NOTE = "Software Interface Specification for  
          the Spherical Harmonics Binary Data  
          Record (SHBDR) file. "  
END\_OBJECT = TEXT  
END

SOFTWARE INTERFACE SPECIFICATION

SPHERICAL HARMONICS BINARY DATA RECORD (SHBDR)

prepared by

Frank G. Lemoine

Code 698, Planetary Geodynamics Laboratory  
NASA Goddard Space Flight Center  
Greenbelt, Maryland, 20771 USA

Peggy L. Jester  
SGT, Inc / Code 614.1  
NASA GSFC / Wallops Flight Facility  
Wallops Island, VA 23337 USA

Version 1.3  
01 July 2011

DOCUMENT CHANGE LOG

REVISION NUMBER	REVISION DATE	SECTION AFFECTED	REMARK
1.0	06/02/20	All	Adapted MGS SHBDR SIS to include Mars Reconnaissance Orbiter and MESSENGER.
1.0	06/03/15	All	Miscellaneous edits
1.0	06/06/29	All	Integrate PDS review comments
1.1	05/04/29	All	Fix minor formatting issues
1.2	08/07/28	2.3	Updated file naming convention for MRO
1.3	11/07/01	4.2.2.3 4.2.2.4	Added NOTE for LP re-analyzed data sets

## Contents

Document Change Log.....	ii
Contents.....	iii
Acronyms and Abbreviations.....	v
1. General Description.....	1
1.1. Overview.....	1
1.2. Scope.....	1
1.3. Applicable Documents.....	1
1.4. System Siting.....	2
1.4.1. Interface Location and Medium.....	2
1.4.2. Data Sources, Transfer Methods, and Destinations.....	2
1.4.3. Generation Method and Frequency.....	3
1.5. Assumptions and Constraints.....	3
1.5.1. Usage Constraints.....	3
1.5.2. Priority Phasing Constraints.....	3
1.5.3. Explicit and Derived Constraints.....	3
1.5.4. Documentation Conventions.....	3
1.5.4.1. Data Format Descriptions.....	3
1.5.4.2. Time Standards.....	4
1.5.4.3. Coordinate Systems.....	4
1.5.4.4. Limits of This Document.....	4
1.5.4.5. Typographic Conventions.....	4
2. Interface Characteristics.....	5
2.1. Hardware Characteristics and Limitations.....	5
2.1.1. Special Equipment and Device Interfaces.....	5
2.1.2. Special Setup Requirements.....	5
2.2. Volume and Size.....	5
2.3. Labeling and Identification.....	5
2.4. Interface Medium Characteristics.....	6
2.5. Failure Protection, Detection, and Recovery Procedures.....	6
2.6. End-of-File Conventions.....	6
3. Access.....	7
3.1. Programs Using the Interface.....	7
3.2. Synchronization Considerations.....	7
3.2.1. Timing and Sequencing Considerations.....	7
3.2.2. Effective Duration.....	7
3.2.3. Priority Interrupts.....	7
3.3. Input/Output Protocols, Calling Sequences.....	7
4. Detailed Interface Specifications.....	8
4.1. Structure and Organization Overview.....	8
4.2. Detached PDS Label.....	8
4.2.1. Label Header.....	8
4.2.2. TABLE Object Definitions.....	11
4.2.2.1. SHBDR Header Object Definition.....	11
4.2.2.2. SHBDR Names Object Definition.....	13
4.2.2.3. SHBDR Coefficient Object Definition.....	14
4.2.2.4. SHBDR Covariance Object Definition.....	15
4.3. Data File.....	16
4.3.1. SHBDR Header Object/Block.....	16
4.3.2. SHBDR Name Block.....	17
4.3.3. SHBDR Coefficients Block.....	17
4.3.4. SHBDR Covariances Block.....	18
5. Support Staff and Cognizant Personnel.....	19

Appendix A. Description of Spherical Harmonic Model Normalization...	A-1
A.1 Definition of Model for the Potential.....	A-1
A.2 Definition of the normalization used.....	A-2
 Appendix B. Binary Data Format.....	 B-1
B.1. IEEE Integer Fields.....	B-1
B.2. IEEE Floating-Point Fields.....	B-1
 Appendix C. Example Data Products.....	 C-1
C.1. Example Label.....	C-1
C.2. Example Data Object.....	C-6
 Tables	
4-3-1. SHBDR Header Block.....	16
4-3-2. SHBDR Names Block.....	17
4-3-3. SHBDR Coefficients Block.....	17
4-3-4. SHBDR Covariance Block.....	18
 Figures	
4-2-1. SHBDR Label Header.....	9

## ACRONYMS AND ABBREVIATIONS

ANSI	American National Standards Institute
APL	Applied Physics Laboratory
ARC	Ames Research Center
ARCDR	Altimetry and Radiometry Composite Data Record
ASCII	American Standard Code for Information Interchange
CCSDS	Consultative Committee for Space Data Systems
CD-WO	Compact-disc write-once
CNES	Centre National d'Etudes Spatiales
CR	Carriage Return
dB	Decibel
DSN	Deep Space Network
DVD	Digital Video Disc or Digital Versatile Disc
EGM96	Earth Gravitational Model 1996
FEA	Front End Assembly
GSFC	Goddard Space Flight Center
IEEE	Institute of Electrical and Electronic Engineers
IAU	International Astronomical Union
JHU	Johns Hopkins University
JPL	Jet Propulsion Laboratory
J2000	IAU Official Time Epoch
K	Degrees Kelvin
kB	Kilobytes
km	Kilometers
LAST	Laser Altimeter Science Team (MESSENGER)
LF	Line Feed
LP	Lunar Prospector (mission or spacecraft)
MB	Megabytes
MESSENGER	MERCURY Surface Space ENVIRONMENT, GEOCHEMISTRY, and RANGING (acronym for mission to Mercury)
MGN	Magellan
MGS	Mars Global Surveyor
MIT	Massachusetts Institute of Technology
MLA	MESSENGER Laser Altimeter
MO	Mars Observer
MRO	Mars Reconnaissance Orbiter
NAIF	Navigation and Ancillary Information Facility
NASA	National Aeronautics and Space Administration
NAV	Navigation Subsystem/Team
ODL	Object Definition Language (PDS)
PDB	Project Data Base
PDS	Planetary Data System
RST	Radio Science Team
SCET	Space Craft Event Time
SFDU	Standard Formatted Data Unit
SHADR	Spherical Harmonics ASCII Data Record
SHBDR	Spherical Harmonics Binary Data Record
SHM	Spherical Harmonics Model
SIS	Software Interface Specification
SPARC	Sun Scaleable Processor Architecture
SPK	Spacecraft and Planet Kernel Format, from NAIF
TBD	To Be Determined
UTC	Universal Time Coordinated

## 1. GENERAL DESCRIPTION

### 1.1. Overview

This Software Interface Specification (SIS) describes Spherical Harmonics Binary Data Record (SHBDR) files. The SHBDR is intended to be general and may contain coefficients for spherical harmonic expansions of gravity, topography, magnetic, and other fields.

### 1.2. Scope

The format and content specifications in this SIS apply to all phases of the project for which a SHBDR is produced.

The SHBDR was defined initially for gravity models derived from Magellan (MGN and Mars Observer (MO) radio tracking data [1], but the format is more generally useful. The original SHBDR has been adapted for the Mars Global Surveyor (MGS) and the Lunar Prospector (LP) missions; this is the adaptation for the Mars Reconnaissance Orbiter (MRO) and MESSENGER missions. Specifics of the various models are included in [2], which will be updated as data for new spherical harmonic models are incorporated within the SHADR definition. A Spherical Harmonic ASCII Data Record is also defined [3], which may be more suitable when error covariances are not included in the final product.

This version adds a note to the object definitions to accommodate new models generated from LP and other historical data[16].

The Jet Propulsion Laboratory (JPL), Pasadena, California, manages the Mars Reconnaissance Orbiter Mission [4], and the Mars Global Surveyor Mission for the National Aeronautics and Space Administration (NASA). The Johns Hopkins University, Laurel, Maryland, USA manages the MESSENGER mission [5,6] for NASA.

### 1.3. Applicable Documents

[1] Tyler, G.L., G. Balmino, D.P. Hinson, W.L. Sjogren, D.E. Smith, R. Woo, S.W. Asmar, M.J. Connally, C.L. Hamilton, and R.A. Simpson, Radio Science Investigations with Mars Observer, *J. Geophys. Res.*, 97, 7759-7779, 1992.

[2] Simpson, R.A., Interpretation and Use of Spherical Harmonics ASCII Data Record (SHADR) and Spherical Harmonics Binary Data Record (SHBDR), Version 1.0, 1993.

[3] Lemoine, F.G., Software Interface Specification: Spherical Harmonics ASCII Data Record (SHADR), 2006.

[4] Mars Reconnaissance Orbiter Mission Plan, Revision C: July 2005, prepared by Robert Lock. Document JPL D-22239, MRO-31-201.

[5] McAdams, J. V. (JHU/APL), MESSENGER mission overview and trajectory design, American Institute of Aeronautics and Astronautics, American Astronautical Society (AIAA/AAS) Astrodynamics Specialist Conference, Paper AAS 03-541, 20 pp., Big Sky, MT, August 3-7, 2003.

[6] McAdams, J. V., D. W. Dunham, R. W. Farquhar, A. H. Taylor, and B. G. Williams, Trajectory design and maneuver strategy for the MESSENGER mission to Mercury, 15th American Astronautical Society (AAS)/American Institute of Aeronautics and Astronautics (AIAA) Space Flight Mechanics

Conference, Paper AAS 05-173, 21 pp., Copper Mountain, CO, Jan. 23-27, 2005.

[7] Seidelmann, P.K., V.K. Abalakin, M. Bursa, M. E. Davies, C. de Bergh, J. H. Lieske, J. Oberst, J. L. Simon, E. M. Standish, P. Stooke, P. C. Thomas, Report of the IAU/IAG Working Group on Cartographic Coordinates and Rotational Elements of the Planets and Satellites: 2000, *Celes. Mechanics and Dyn. Astronomy*, 82, 83-110, Dec 2002.

[8] MRO-D-22685, Rev B., Planetary Constants and Models, 05-15-2003.

[9] Konopliv, A.S, C.F. Yoder, E. M. Standish, D.-N. Yuan, and W. L. Sjogren, A global solution for the Mars static and seasonal gravity, Mars orientation, Phobos, Deimos Masses, and Mars Ephemeris, *Icarus*, 182(1), 23-50, 2006.

[10] Konopliv A.S., S.W. Asmar, E. Carranza, W.L. Sjogren, and D.N. Yuan, Recent Gravity models as a results of the Lunar Prospector Mission, *Icarus*, 150, 1-18, 2001.

[11] Lambeck, Kurt, *Geophysical Geodesy*, Oxford University Press, Oxford, UK, 1988.

[12] Kaula, William M., *Theory of Satellite Geodesy, Applications of satellites to geodesy*, Dover Publications, Mineola, NY, 2000.

[13] Lemoine, F.G., S.C. Kenyon, J.K. Factor, R.G. Trimmer, N.K. Pavlis, C.M. Cox, S.M. Klosko, S.B. Luthcke, M.H. Torrence, Y.M. Wang, R.G. Williamson, E.C. Pavlis, R.H. Rapp and T.R. Olson, The Development of the Joint NASA GSFC and the National Imagery and Mapping Agency (NIMA) Geopotential Model EGM96, NASA/TP-1998-206861, NASA Goddard Space Flight Center, Greenbelt, Maryland 20771, July 1998.

[14] JPL D-7116, Rev. E, Planetary Science Data Dictionary Document, Jet Propulsion Laboratory, Pasadena, California, August 28, 2002. (<http://pds.jpl.nasa.gov/documents/psdd/psdd.pdf>)

[15] JPL D-7669 Part 2, Planetary Data System Standards Reference, PDS Version 3.6, Jet Propulsion Laboratory, August 1, 2003. (<http://pds.jpl.nasa.gov/documents/sr/index.html>)

[16] Mazarico, E., F. G. Lemoine, S.-C. Han, and D. E. Smith ( 2010 ), GLGM-3: A degree-150 lunar gravity model from the historical tracking data of NASA Moon orbiters , *J. Geophys. Res.* , 115 , E05001, doi:10.1029/2009JE003472

#### 1.4. System Siting

##### 1.4.1. Interface Location and Medium

SHBDR files are created at the institution conducting the science analysis. SHBDR files can be electronic files or can be stored on compact-disc write-once (CD-WO) or DVD type media.

##### 1.4.2. Data Sources, Transfer Methods, and Destinations

SHBDR files are created from radio tracking, vertical sounding, in situ, and/or other measurements at the institution conducting the scientific data analysis. They are transferred to and deposited in a data system (such as the PDS) specified by the managing institution.

### 1.4.3. Generation Method and Frequency

Spherical Harmonic Models are developed separately at each institution conducting scientific analyses on raw data; each model meets criteria specified by the investigators conducting the analysis. Each model requires data with complete sampling (in terms of longitude and latitude coverage on the planet), so that SHBDR files will be issued infrequently and on schedules which cannot be predicted at this time.

## 1.5. Assumptions and Constraints

### 1.5.1. Usage Constraints

None.

### 1.5.2. Priority Phasing Constraints

None.

### 1.5.3. Explicit and Derived Constraints

None.

### 1.5.4. Documentation Conventions

#### 1.5.4.1. Data Format Descriptions

The reference data unit is the byte. Data may be stored in fields with various sizes and formats, viz. one-, two-, and four-byte binary integers, four- and eight-byte binary floating-point numbers, and character strings. Data are identified throughout this document as

char	8 bits	character
uchar	8 bits	integer
short	16 bits	integer
long	32 bits	integer
float	32 bits	floating point (sign, exponent, and mantissa)
double	64 bits	floating point (sign, exponent, and mantissa)
u (prefix)		unsigned (as with ulong for unsigned 32-bit integer)
other		special data structures such as time, date, etc. which are described within this document

If a field is described as containing *n* bytes of ASCII character string data, this implies that the leftmost (lowest numbered) byte contains the first character, the next lowest byte contains the second character, and so forth.

An array of *n* elements is written as `array[n]`; the first element is `array[0]`, and the last is `array[n-1]`. `array[n][m]` describes an *n* x *m* element array, with first element `array[0][0]`, second element `array[0][1]`, and so forth.

Floating point (real) numbers are represented as double precision character strings in the FORTRAN 1P1E23.16 format. Fixed point (integer) numbers are represented using the FORTRAN I5 format.



#### 1.5.4.2. Time Standards

SHBDR files use the January 1.5, 2000 epoch as the standard time. Within the data files, all times are reported in Universal Coordinated Time (UTC) as strings of 23 ASCII characters. The time format is "YYYY-MM-DDThh:mm:ss.fff", where "-", "T", ":", and "." are fixed delimiters; "YYYY" is the year "19nn" or "20nn"; "MM" is a two-digit month of year; "DD" is a two-digit day of month; "T" separates the date and time segments of the string; "hh" is hour of day; "mm" is the minutes of hour (00-59); "ss" is the seconds of minute (00-59); and "fff" is fractional seconds in milliseconds.

The date format is "YYYY-MM-DD", where the components are defined as above.

#### 1.5.4.3. Coordinate Systems

The SHBDR uses the appropriate planetocentric fixed body coordinate system [7,8]. This may be an IAU system (e.g. IAU2000 [7] or for the new body-fixed Mars reference frame defined by Konopliv et al. [9]). At present, the MESSENGER mission has adopted the IAU2000 model for Mercury [7].

The coordinate system for lunar geopotential models will be a body figure axis system defined by the lunar librations, which are resolved by lunar laser ranging [10], or a coarser frame defined by the IAU [7].

#### 1.5.4.4. Limits of This Document

This document applies only to SHBDR data files.

#### 1.5.4.5. Typographic Conventions

This document has been formatted for simple electronic file transfer and display. Line lengths are limited to approximately 80 ASCII characters, including line delimiters. No special fonts or structures are included within the file. Constant width characters are assumed for display.

## 2. INTERFACE CHARACTERISTICS

### 2.1. Hardware Characteristics and Limitations

#### 2.1.1. Special Equipment and Device Interfaces

Users of the SHBDR product must have access to the data system (or to media) on which SHBDR files are stored.

#### 2.1.2. Special Setup Requirements

None.

### 2.2. Volume and Size

SHBDR products have variable length, depending on the degree and order of the model and the number of tables included. A model of degree and order  $N$  will include approximately  $N^2$  terms and therefore the number of terms in the covariance matrix will be of order  $N^4$ . For 8-byte storage and  $N=50$ , the total SHBDR volume will be about 30 MB. For  $N=100$ , the total SHBDR volume will be approximately 416 MB.

Vector quantities (e.g., magnetic field) may be described by a single SHBDR (in which all components are represented) or by a separate SHBDR for each field component. If the single SHBDR includes covariances, the file size will be approximately 27 times larger than the combined volumes of the three component files because of the inter-component covariance terms.

In general, the SHBDR is recommended over the SHADR [3] when the data include error covariances because of the smaller data volume associated with binary formats.

### 2.3. Labeling and Identification

The length of file names is limited to 27 or less characters before the period delimiter and 3 characters after the period delimiter.

Each file has a name which describes its contents. The name includes the following structure which uniquely identifies it among SHBDR products. Beginning with the MRO gravity products the following file naming convention is used:

GTsss\_nnnnvv\_SHB.DAT

where

- "G" denotes the generating institution
  - "J" for the Jet Propulsion Laboratory
  - "G" or Goddard Space Flight Center
  - "C" or Centre National d'Etudes Spatiales
  - "M" for Massachusetts Institute of Technology
- "T" indicates the type of data represented
  - "G" for gravity field
  - "T" for topography
  - "M" for magnetic field
- "sss" is a 3-character modifier specified by the data producer. This modifier is used to indicate the source spacecraft or Project, such as MRO for the Mars Reconnaissance Orbiter.

"\_" the underscore character is used to delimit modifiers in the file name for clarity.

"nnnnvv" is a 4- to 6-character modifier specified by the data producer. Among other things, this modifier may be used to indicate the target body, whether the SHBDR contains primary data values as specified by "T" or uncertainties/errors, and/or the version number. For MRO, this modifier indicates the degree and order of the solution for the gravity field, topography or magnetic field.

"\_" the underscore character is used to delimit modifiers in the file name for clarity.

"SHB" denotes that this is a Binary file of Spherical Harmonic coefficients and error covariance information

".DAT" indicates the data is stored in binary format.

Each SHBDR file is accompanied by a detached PDS label; that label is a file in its own right, having the name GTsss\_nnnnvv\_SHB.LBL.

#### 2.4. Interface Medium Characteristics

SHBDR products are electronic files.

#### 2.5. Failure Protection, Detection, and Recovery Procedures

None.

#### 2.6. End-of-File Conventions

End of file labeling complies with standards for the medium on which the files are stored.

### 3. ACCESS

#### 3.1. Programs Using the Interface

Data contained in SHBDR files will be accessed by programs at the home institutions of science investigators. Those programs cannot be identified here.

#### 3.2. Synchronization Considerations

##### 3.2.1. Timing and Sequencing Considerations

N/A

##### 3.2.2. Effective Duration

N/A

##### 3.2.3. Priority Interrupts

None.

#### 3.3. Input/Output Protocols, Calling Sequences

None.

## 4. DETAILED INTERFACE SPECIFICATIONS

### 4.1. Structure and Organization Overview

The SHBDR is a file generated by software at the institution conducting scientific data analysis. Each SHBDR file is accompanied by a detached PDS label.

### 4.2. Detached PDS Label

The detached PDS label is a file with two parts -- a header, and a set of one to four PDS TABLE object definitions. The header contains information about the origin of the file and its general characteristics such as record type and size. The TABLE object definitions describe the format and content of the tables that make up the SHBDR data file. The SHBDR Header Table Object definition is required. The SHBDR Names Object Definition is required if there is an SHBDR Names Object in the file. The SHBDR Coefficients Table Object definition is required if there is a SHBDR Coefficients Table in the file; the SHBDR Covariance Table Object definition is required if there is a SHBDR Covariance Table.

Each detached PDS label is constructed of ASCII records; each record in the label contains exactly 80 characters. The last two characters in each record are the carriage-return (ASCII 13) and line-feed (ASCII 10) characters.

An example of a complete label and data object is given in Appendix C.

#### 4.2.1 Label Header

The structure of the label header is illustrated in Figure 4-2-1. Keyword definitions are given below.

PDS\_VERSION\_ID =

The version of the Planetary Data System for which these data have been prepared; set to PDS3 by agreement between the mission and PDS.

RECORD\_TYPE =

The type of record. Set to "FIXED\_LENGTH" to indicate that all logical records have the same length.

RECORD\_BYTES =

The number of bytes per (fixed-length) record.

FILE\_RECORDS =

The number of records in the SHBDR file: instance dependent.

^SHBDR\_HEADER\_TABLE=

File name and record number at which SHBDR\_HEADER\_TABLE begins. Set to ("GTsss\_nnnnvv\_SHB.DAT ",1) where "GTsss\_nnnnvv\_SHB.DAT " is the file name as described in Section 2.3, and 1 is the record number since this is the first record in the SHBDR file.

Figure 4-2-1 SHBDR Label Header

```

PDS_VERSION_ID = PDS3
RECORD_TYPE = FIXED_LENGTH
RECORD_BYTES = nnn
FILE_RECORDS = nnn
^SHBDR_HEADER_TABLE = ("GTsss_nnnnvv_SHB.DAT",1)
^SHBDR_NAMES_TABLE = ("GTsss_nnnnvv_SHB.DAT ",1)
^SHBDR_COEFFICIENTS_TABLE = ("GTsss_nnnnvv_SHB.DAT ",nn)
^SHBDR_COVARIANCE_TABLE = ("GTsss_nnnnvv_SHB.DAT ",nnn)
INSTRUMENT_HOST_NAME = "cccccccccccccccccccc"
TARGET_NAME = "cccc"
INSTRUMENT_NAME = "cccccccccccccccccccccccc"
DATA_SET_ID = "cccccccccccccccccccccccc"
OBSERVATION_TYPE = "cccccccccccccccc"
ORIGINAL_PRODUCT_ID = "cccccccccccccccc"
PRODUCT_ID = "GTnnnnnvv.SHB"
PRODUCT_RELEASE_DATE = YYYY-MM-DD
DESCRIPTION = "cccccccccccccccccccc"
START_ORBIT_NUMBER = nnnn
STOP_ORBIT_NUMBER = nnnn
START_TIME = YYYY-MM-DDThh:mm:ss
STOP_TIME = YYYY-MM-DDThh:mm:ss
PRODUCT_CREATION_TIME = YYYY-MM-DDThh:mm:ss.fff
PRODUCER_FULL_NAME = "cccccccccccc"
PRODUCER_INSTITUTION_NAME = "cccccccccccc"
PRODUCT_VERSION_TYPE = "cccccccccccc"
PRODUCER_ID = "cccccccc"
SOFTWARE_NAME = "cccccccc;Vn.m"

```

**^SHBDR\_NAMES\_TABLE =**  
File name and record number at which the SHBDR\_NAMES\_TABLE begins. The Names Table is required if the Coefficients Table is included in the file. This pointer will not appear in the SHBDR label if there are no Coefficients Table. Set to ("GTsss\_nnnnvv\_SHB.DAT ",nn) where "GTsss\_nnnnvv\_SHB.DAT " is the file name as described in Section 2.3, and "nn" is the record number in the file where the Names Table begins.

**^SHBDR\_COEFFICIENTS\_TABLE=**  
File name and record number at which SHBDR\_COEFFICIENTS\_TABLE begins. The Coefficients Table is optional; this pointer will not appear in the SHBDR label if there is no Coefficients Table. Set to ("GTsss\_nnnnvv\_SHB.DAT ",nn) where "GTsss\_nnnnvv\_SHB.DAT " is the file name as described in Section 2.3, and "nn" is the record number in the file where the Coefficients Table begins.

**^SHBDR\_COVARIANCE\_TABLE=**  
File name and record number at which SHBDR\_COVARIANCE\_TABLE begins. The Covariance Table is optional; this pointer will not appear in the SHBDR label if there is no Covariance Table. Set to ("GTsss\_nnnnvv\_SHB.DAT ",nn) where "GTsss\_nnnnvv\_SHB.DAT " is the file name as described in Section 2.3, and "nn" is the record number in the file where the Covariance Table begins.

**INSTRUMENT\_HOST\_NAME =**  
Name of the spacecraft; acceptable names include "MARS GLOBAL SURVEYOR"

"LUNAR PROSPECTOR", "MARS RECONNAISSANCE ORBITER", and "MERCURY SURFACE, SPACE, ENVIRONMENT, GEOCHEMISTRY, AND RANGING".

TARGET\_NAME =

A character string that identifies the target body. For MRO- and MGS-derived SHBDR files, the character string will be "MARS". For MESSENGER SHBDR files the character string will be "MERCURY". For Lunar Prospector SHBDR files, the character string will be "MOON".

INSTRUMENT\_NAME =

Name of the instrument; set to "RADIO SCIENCE SUBSYSTEM" for products generated from radio science data, or set to other instrument names as appropriate.

DATA\_SET\_ID =

Identifier for the data set of which this SHBDR product is a member.  
-Set to "MRO-M-RSS-5-SDP-Vn.m" for Mars Reconnaissance Orbiter;  
-Set to "MESS-H-RSS-5-SDP-Vn.m" for MESSENGER;  
-Set to "MGS-M-RSS-5-SDP-Vn.m" for MGS; and "  
-Set to "LP-L-RSS-5-GLGM3/GRAVITY-Vn.m" for Lunar Prospector;  
The suffix Vn.m indicates the version number of the data set.

OBSERVATION\_TYPE =

A character string that identifies the data in the product. For the spherical harmonic model of a gravity field, the character string "GRAVITY FIELD". For a model of planet topography, the character string "TOPOGRAPHY".

ORIGINAL\_PRODUCT\_ID =

Optional. An identifier for the product provided by the producer. Generally a file name, different from PRODUCT\_ID, which would be recognized at the producer's home institution.

PRODUCT\_ID =

A unique identifier for the product within the collection identified by DATA\_SET\_ID. Generally, the file name used in pointers ^SHBDR\_HEADER\_TABLE. The naming convention is defined in Section 2.3.

PRODUCT\_RELEASE\_DATE =

The date on which the product was released to the Planetary Data System; entered in the format "YYYY-MM-DD", where components are defined in Section 1.5.4.2.

DESCRIPTION =

A short description of the SHBDR product.

START\_ORBIT\_NUMBER =

Optional. The first orbit represented in the SHBDR product. An integer.

STOP\_ORBIT\_NUMBER =

Optional. The last orbit represented in the SHBDR product. An integer.

START\_TIME =

Optional. The date/time of the first data included in the model, expressed in the format "YYYY-MM-DDThh:mm:ss" where the components are defined in section 1.5.4.2.

STOP\_TIME =

Optional. The date/time of the last data included in the model, expressed

in the format "YYYY-MM-DDThh:mm:ss" where the components are defined in section 1.5.4.2.

PRODUCT\_CREATION\_TIME =

The time at which this SHBDR was created; expressed in the format "YYYY-MM-DDThh:mm:ss.fff" where the components are defined in Section 1.5.4.2.

PRODUCER\_FULL\_NAME=

The name of the person primarily responsible for production of this SHBDR file. Expressed as a character string, for example "JOHANNES KEPLER".

PRODUCER\_INSTITUTION\_NAME=

The name of the institution primarily responsible for production of this SHADR. Standard values include:

"STANFORD UNIVERSITY"  
"GODDARD SPACE FLIGHT CENTER"  
"JET PROPULSION LABORATORY"  
"CENTRE NATIONAL D'ETUDES SPATIALES"  
"MASSACHUSETTS INSTITUTE OF TECHNOLOGY"

PRODUCT\_VERSION\_TYPE=

The version of this SHBDR.  
Standard values include "PREDICT", "PRELIMINARY", and "FINAL".

PRODUCER\_ID =

The entity responsible for creation of the SHBDR product. For products generated by the Mars Reconnaissance Orbiter Gravity Science Team set to "MRO GST". For products generated by the MESSENGER Laser Altimeter Science Team, set to "MESS LAST". For products generated by the Mars Global Surveyor Radio Science Team, set to "MGS RST".

SOFTWARE\_NAME =

The name and version number of the program creating this SHBDR file; expressed as a character string in the format "PROGRAM\_NAME;n.mm" where "PROGRAM\_NAME" is the name of the software and "n.mm" is the version number. (e.g. "SOLVE;200201.02")

#### 4.2.2 TABLE Object Definitions

##### 4.2.2.1 SHBDR Header Object Definition

Each SHBDR Header Object is completely defined by the Header Object Definition in its Label. The definition which follows gives the structure of the Header Object; some of the DESCRIPTION values may vary from product to product. The SHBDR Header Object Definition is a required part of the SHBDR label file. It immediately follows

```
OBJECT = SHBDR_HEADER_TABLE
ROWS = 1
COLUMNS = 9
ROW_BYTES = 56
INTERCHANGE_FORMAT = BINARY
DESCRIPTION = "The SHBDR header includes descriptive
information about the spherical harmonic coefficients that follow in
SHBDR_COEFFICIENTS_TABLE. The header consists of a single record of
nine data columns requiring 56 bytes. The Header is followed by a
pad of binary integer zeroes to ensure alignment with RECORD_BYTES."
OBJECT = COLUMN
NAME = "REFERENCE RADIUS"
```



```

DATA_TYPE          = IEEE_REAL
START_BYTE         = 1
BYTES              = 8
UNIT               = "KILOMETER"
DESCRIPTION        = "The assumed reference radius
of the spherical planet."
END_OBJECT = COLUMN

OBJECT = COLUMN
NAME               = "CONSTANT"
DATA_TYPE          = IEEE_REAL
START_BYTE         = 9
BYTES              = 8
UNIT               = "KM^3/S^2"
DESCRIPTION        = "For a gravity field model
the assumed gravitational constant GM in kilometers cubed per seconds
squared for the planet. For a topography model, set to 1."
END_OBJECT = COLUMN

OBJECT = COLUMN
NAME               = "UNCERTAINTY IN CONSTANT"
DATA_TYPE          = IEEE_REAL
START_BYTE         = 17
BYTES              = 8
UNIT               = "KM^3/S^2"
DESCRIPTION        = "For a gravity field model the uncertainty
in the gravitational constant GM in kilometers cubed per seconds squared
for the planet. For a topography, set to 0."
END_OBJECT = COLUMN

OBJECT = COLUMN
NAME               = "DEGREE OF FIELD"
DATA_TYPE          = MSB_INTEGER
START_BYTE         = 25
BYTES              = 4
UNIT               = "N/A"
DESCRIPTION        = "The degree of model field."
END_OBJECT = COLUMN

OBJECT = COLUMN
NAME               = "ORDER OF FIELD"
DATA_TYPE          = MSB_INTEGER
START_BYTE         = 29
BYTES              = 4
UNIT               = "N/A"
DESCRIPTION        = "The order of the model field."
END_OBJECT = COLUMN

OBJECT = COLUMN
NAME               = "NORMALIZATION STATE"
DATA_TYPE          = MSB_INTEGER
START_BYTE         = 33
BYTES              = 4
UNIT               = "N/A"
DESCRIPTION        = "The normalization indicator.
For gravity field:
0 coefficients are unnormalized
1 coefficients are normalized
2 other."
END_OBJECT= COLUMN

```

```

OBJECT = COLUMN
  NAME = "NUMBER OF NAMES"
  DATA_TYPE = MSB_INTEGER
  START_BYTE = 37
  BYTES = 4
  UNIT = "N/A"
  DESCRIPTION = "Number of valid names in the SHBDR Names
Table. Also, the number of valid coefficients in the SHBDR
Coefficients Table."
END_OBJECT = COLUMN

```

```

OBJECT = COLUMN
  NAME = "REFERENCE LONGITUDE"
  POSITIVE_LONGITUDE_DIRECTION = "EAST"
  DATA_TYPE = IEEE_REAL
  START_BYTE = 41
  BYTES = 8
  UNIT = "DEGREE"
  DESCRIPTION = "The reference longitude
for the spherical harmonic expansion; normally 0."
END_OBJECT = COLUMN

```

```

OBJECT = COLUMN
  NAME = "REFERENCE LATITUDE"
  DATA_TYPE = IEEE_REAL
  START_BYTE = 49
  BYTES = 23
  FORMAT = "E23.16"
  UNIT = "DEGREE"
  DESCRIPTION = "The reference latitude
for the spherical harmonic expansion; normally 0."
END_OBJECT = COLUMN

```

```
END_OBJECT = SHBDR_HEADER_TABLE
```

#### 4.2.2.2 SHBDR Names Object Definition

The SHBDR Names Object is completely defined by the Names Object Definition in the label. The definition below illustrates general structural form. The SHBDR Names Object is an optional part of the SHBDR file. If the Names Object is not included, either the Names Object Definition will be omitted or the number of rows will be set to zero (ROWS = 0). If the Names Object is not included, the pointer ^SHBDR\_NAMES\_TABLE will not appear in the Standard Keywords and Values. If the Coefficients Object is included in the SHBDR file, the Names Object is required.

```

OBJECT = SHBDR_NAMES_TABLE
  ROWS = *
  COLUMNS = 1
  ROW_BYTES = 8
  INTERCHANGE_FORMAT = BINARY
  DESCRIPTION = "The SHBDR Names Table contains names
for the solution parameters (including gravity field coefficients) which
will follow in the SHBDR_COEFFICIENTS_TABLE. The order of the names
in the SHBDR_NAMES_TABLE corresponds identically to the order
of the parameters in the SHBDR_COEFFICIENTS_TABLE. Each coefficient
name is of the form Cnm or Snm where n is the degree of the
coefficient and m is the order of the coefficient.
Both indices are three-digit zero-filled right-justified ASCII

```

character strings (for example, C010005 for the 10th degree 5th order C coefficient, or S002001 for the 2nd degree 1st order S coefficient). The eighth byte in the table is an ASCII blank used to ensure that the row length is equal to RECORD\_BYTES. Names of other solution parameters are limited to 8 ASCII characters; if less than 8, they will be left-justified and padded with ASCII blanks. The Names Table itself will be padded with ASCII blanks, if necessary, so that its length is an integral multiple of RECORD\_BYTES."

```

OBJECT = COLUMN
    NAME           = "PARAMETER NAME"
    DATA_TYPE     = CHARACTER
    START_BYTE     = 1
    BYTES          = 8
    UNIT           = "N/A"
    DESCRIPTION    = "The name of the coefficient or other
solution parameter, left-justified and padded with ASCII blanks
(if needed) to 8 characters."
END_OBJECT = COLUMN
END_OBJECT = SHBDR_NAMES_TABLE

```

#### 4.2.2.3 SHBDR Coefficients Object Definition

The SHBDR Coefficients Object is completely defined by the Coefficients Object Definition in the label. Small differences in DESCRIPTION values should be expected from product to product. The structure outlined in the Definition below should not vary, however.

The SHBDR Coefficients Object is an optional part of the SHBDR data file. This allows the SHBDR to be used for targets which are too small or too remote to have easily discerned coefficients, but for which estimates of mass have been obtained (e.g., satellites Phobos and Deimos). If the Covariance Object is included in the SHBDR, the Coefficients Object is required.

If the Coefficients Object is not included in the SHBDR file, either the SHBDR Coefficients Object Definition will be omitted or the number of rows will be set to zero (ROWS = 0). If the SHBDR Coefficients Object is not included, the pointer ^SHBDR\_COEFFICIENTS\_TABLE will not appear in the label header. If the SHBDR Coefficients Object Definition is included in the label, it immediately follows the SHBDR Names Object Definition.

NOTE: For Lunar Prospector data modelled with GLGM-3 the data is in little-endian format and the covariance data is a row ordered upper triangular matrix.

The order in which coefficients appear in the Coefficients Object is defined by the Names Object [2].

```

OBJECT = SHBDR_COEFFICIENTS_TABLE
    ROWS           = *
    COLUMNS       = 1
    ROW_BYTES      = 8
    INTERCHANGE_FORMAT = BINARY
    DESCRIPTION    = "The SHBDR Coefficients Table
contains the coefficients and other solution parameters
for the spherical harmonic model. The order of the
coefficients in this table corresponds exactly to the
order of the coefficient and parameter names in

```

SHBDR\_NAMES\_TABLE. The SHBDR Coefficients Table will be padded with double precision DATA\_TYPE zeroes so that its total length is an integral multiple of RECORD\_BYTES."

```
OBJECT = COLUMN
  NAME           = "COEFFICIENT VALUE"
  DATA_TYPE     = *
  START_BYTE    = 1
  BYTES         = 8
  UNIT          = "N/A"
  DESCRIPTION    = "A coefficient Cnm or
  Snm or other solution parameter as specified in the
  SHBDR Names Table."
END_OBJECT = COLUMN
END_OBJECT = SHBDR_COEFFICIENTS_TABLE
```

#### 4.2.2.4 SHBDR Covariance Object Definition

The SHBDR Covariance Object is completely defined by the Covariance Object Definition in the label. Small differences in DESCRIPTION values should be expected from product to product. The structure established by the Definition below should not change, however.

The SHBDR Covariance Object is an optional part of the SHBDR data file. If the Covariance Object is not included, either the Covariance Object Definition will be omitted or the number of rows will be set to zero (ROWS = 0). If the SHBDR Covariance Object is not included, the pointer ^SHBDR\_COVARIANCE\_TABLE will not appear in the label header. If the SHBDR Covariance Object Definition is included in the label, it immediately follows the SHBDR Coefficients Object Definition.

NOTE: For Lunar Prospector data modelled with GLGM-3 the data is in little-endian format and the covariance data is a row ordered upper triangular matrix.

The order in which covariance terms appear in the Covariance Object is defined by the Names Object [2].

```
OBJECT = SHBDR_COVARIANCE_TABLE
  ROWS           = *
  COLUMNS       = 1
  ROW_BYTES     = 8
  INTERCHANGE_FORMAT = BINARY
  DESCRIPTION    = "The SHBDR Covariance Table
  contains the covariances for the spherical harmonic model
  coefficients and other solution parameters. The order of
  the covariances in this table is defined by the product
  of the SHBDR Names Table with its transpose, except that
  redundant terms are omitted on their second occurrence.
  The SHBDR Covariance Table will be padded with double
  precision DATA_TYPE zeroes so that its total length is
  an integral multiple of RECORD_BYTES."
```

```
OBJECT = COLUMN
  NAME           = "COVARIANCE VALUE"
  DATA_TYPE     = *
  START_BYTE    = 1
  BYTES         = 8
```

```

UNIT                = "N/A"
DESCRIPTION         = "The covariance value
for the coefficients and other solution parameters
specified by the product of SHBDR_NAMES_TABLE with
its transpose, after omitting redundant terms."
END_OBJECT         = COLUMN

```

```

END_OBJECT         = SHBDR_COVARIANCE_TABLE

```

### 4.3. Data File

Each SHBDR data file comprises one or more data blocks. The data objects were defined in Section 4.2. The data blocks are illustrated below.

The Header Object is required in each SHBDR file; the Names Object, the Coefficients Object, and the Covariance Object are optional. If the Covariance Object is included, both the Coefficients Object and the Names Object are required; if the Coefficients Object is included, the Names Object is required.

#### 4.3.1. SHBDR Header Object/Block

The SHBDR Header Object contains the parameters necessary to interpret the data in the SHBDR file. The structure and content of the SHBDR Header Object are defined in Section 4.2.2.1. The SHBDR Header Object is a one-row table; hence the Header Object and the Header Block are logically synonymous. The structure of the Header Block is shown in Table 4-3-1.

Table 4-3-1. SHBDR Header Block				
Col No	Offset	Length	Format	Column Nam
1	+0	8	double	Planetary Radius
2	8	8	double	Constant
3	16	8	double	Uncertainty in Constant
4	24	4	long	Degree of Field
5	28	4	long	Order of Field
6	32	4	long	Normalization State
7	36	4	long	Number of Names
8	40	8	double	Reference Longitude
9	48	8	double	Reference Latitude
	+56			

#### 4.3.2. SHBDR Names Block

The SHBDR Names Object comprises one or more SHBDR Names Blocks. Each block contains the name of one coefficient or solution parameter in the Spherical Harmonic Model. The structure and content of the SHBDR Names Object are defined in Section 4.2.2.2. The structure of an individual block is shown in Table 4-3-2.

Table 4-3-2. SHBDR Names Block				
Col No	Offset	Length	Format	Column Name
1	+0	8	A8	Coefficient or Solution Parameter Name
	+8			

#### 4.3.3. SHBDR Coefficients Block

The SHBDR Coefficients Object comprises one or more SHBDR Coefficients Blocks. Each block contains the value of one coefficient or other solution parameter for the overall model defined by the SHBDR product. The structure and content of the SHBDR Coefficients Object are defined in Section 4.2.2.3. The structure of an individual block is shown in Table 4-3-3.

Table 4-3-3. SHBDR Coefficients Block				
Col No	Offset	Length	Format	Column Name
1	+0	8	double	Coefficient Cnm or Snm or other solution parameter
	+8			

#### 4.3.4. SHBDR Covariance Block

The SHBDR Covariance Object comprises one or more SHBDR Covariance Blocks. Each SHBDR Covariance Block contains one covariance for the overall model defined by the SHBDR product. The structure and content of the SHBDR Covariance Object are defined in Section 4.2.2.4. The structure of an individual block is shown in Table 4-3-4. The SHBDR Covariance Object is an optional component of the SHBDR file.

Table 4-3-4. SHBDR Covariance Block				
Col No	Offset	Length	Format	Column Name
1	+0	8	double	Covariance Value
	+8			

## 5. SUPPORT STAFF AND COGNIZANT PERSONNEL

The following persons may be contacted for information.

### Mars Reconnaissance Orbiter Gravity Science Team

Frank G. Lemoine  
Code 698, Planetary Geodynamics Laboratory  
NASA Goddard Space Flight Center  
Greenbelt, Maryland 20771 U.S.A.  
Phone: 301-614-6109  
FAX: 301-614-6522  
Electronic mail: Frank.Lemoine@gssc.nasa.gov

### MESSENGER Laser Altimeter Science Team

Maria T. Zuber  
Department of Earth, Atmospheric, and Planetary  
Sciences  
Massachusetts Institute of Technology  
54-918  
Cambridge, MA 02139-4307  
Phone: 617-253-0149  
FAX: 617-253-8298

### Planetary Data System:

PDS Operator  
Planetary Data System  
MS 202-101  
Jet Propulsion Laboratory  
4800 Oak Grove Drive  
Pasadena, CA 91109-8099  
  
Phone: 818-354-4321  
Electronic Mail: pds\_operator@jpl.nasa.gov



## Appendix A. Description of Spherical Harmonic Model Normalization

### A.1 DEFINITION OF SPHERICAL HARMONIC MODELS FOR THE GEOPOTENTIAL.

Spherical harmonics satisfy Laplace's equation in spherical coordinates. The gravity potential field of the planets and the mathematical representation of magnetic fields and topographic fields are readily expressed in terms of spherical harmonics. Useful reviews are by Lambeck [11] (Section 2.2, Elements of Potential Theory) and Kaula [12] (Section 1.1 Potential Theory, and Section 1.2 Spherical Harmonics).

$$V = (GM/r) + (GM/r) \sum_n \sum_m (R_e/r)^{2n} [C_{nm} \cos(mL) + S_{nm} \sin(mL)] P_{nm}(\sin(\phi))$$

(Equation A-1-1)

where GM is the gravitational constant of the planet, r is the radial distance of the test point from the origin, and  $R_e$  is the assumed reference radius of the spherical planet for which the coefficients were calculated. The summations take place from degree  $n=1$  to infinity, and order  $m=0$  to  $n$ ;  $C_{nm}$  and  $S_{nm}$  refer to the normalized spherical harmonic coefficients (see Section A.2 below); L is the longitude; the  $P_{nm}$  are the normalized associated Legendre functions of degree n and order m; and  $\phi$  is the latitude of the test point. If we assume the origin is at the center of mass, the degree one terms vanish, and the summation in degree starts at degree  $n=2$ .

A "solution" for a spherical harmonic model of the geopotential refers to a solution for these spherical harmonic coefficients and the gravitational constant, GM, of the body.

In practice the spherical harmonic series is truncated at a maximum degree  $n_{max}$ . For MRO, the likely degree of truncation will be between  $n=100$  and  $n=120$ . For MESSENGER gravity solutions of the planet Mercury, solutions will likely be truncated at degree 20. The degree of truncation depends on the quality of the tracking data, and the orbits of the spacecraft in the geopotential solution. For Lunar Prospector derived gravity solutions, the maximum degree has ranged from  $n=100$  to  $n=165$  [10].

If the origin is placed at the center of mass, the degree 1 terms vanish from the spherical harmonic expansion, and the first summation above is then from ( $n=2$ ) to the maximum degree,  $n_{max}$ .

Figure 1, section 1.2 from Kaula [11] gives examples of spherical harmonics. The zonal terms,  $m=0$ , have  $n$  zeros in a distance  $\pi$  along a meridian N-S in other words they represent only latitudinal variations in the potential.

Zonal terms may be represented in the literature as  $J_n = -C_{n0}$ .

Aside from GM,  $C_{20}$  is the most significant term in the gravity field (for planets such as the Earth and Mars), and reflects the dynamical expression of the planet's polar flattening.

Tesseral harmonics (coefficients where  $n$  is not equal to  $m$ , and  $m > 0$ , have  $n-m$  zeros in a distance  $\pi$  along a meridian (like the tesserae of a mosaic).

Sectoral harmonics are coefficients where  $n=m$  and are constant in sectors of longitude (N-S) and have  $n$  zero crossings in a distance  $\pi$  along a meridian of latitude (E-W).

## A.2 DEFINITION OF THE NORMALIZATION USED FOR GEOPOTENTIAL COEFFICIENTS.

The normalization for spherical harmonic coefficients is given by Lambeck[11]

$$C_{nm}'' = C_{nm}/PI_{nm}$$

(Equation A-2-1)

where  $C_{nm}''$  is normalized and  $C_{nm}$  is un-normalized, and

$$[PI_{nm}]^{**2} = (2 - \delta_{0m}) * (2n+1) * (n-m)! / (n+m)!$$

(Equation A-2-2)

$\delta_{0m}$  refers to the Kronecker delta function -- unity for coefficients where  $m=0$  (the zonal terms), zero for order  $m > 0$ .

For zonal coefficients ( $m=0$ ) the relation reduces to

$$C_{nm}'' = C_{nm} / \text{sqrt}(2n+1)$$

For example, for the Earth  $C_{20} = -1.08262668355E-03$  (un-normalized) so

$$C_{20}'' = C_{20} / \text{sqrt}(5) = -4.8416537173572E-04 \text{ (normalized)}$$

Working the process backwards for Earth's  $C_{22}$  we have

$$C_{22}'' = .24391435239839D-05$$

(from the Earth Gravitational Model 1996, EGM96, [13])

$$\begin{aligned} [PI_{nm}]^{**2} &= (2-0)*(2n+1) (2-2)! / (4)! \\ &= 2*5*1/(4!) = 5/12 \end{aligned}$$

which yields

$$C_{22} = \text{sqrt}(5/12) * (.24391435239839E-05) = 1.5744604E-06$$

closely matching Lambeck's [11] result (page 14).

Likewise for Earth's  $S_{22}$ , we have  $S_{22}'' = -.14001668365394E-05$

(normalized from the Earth Gravitational Model 1996, EGM96, [13])

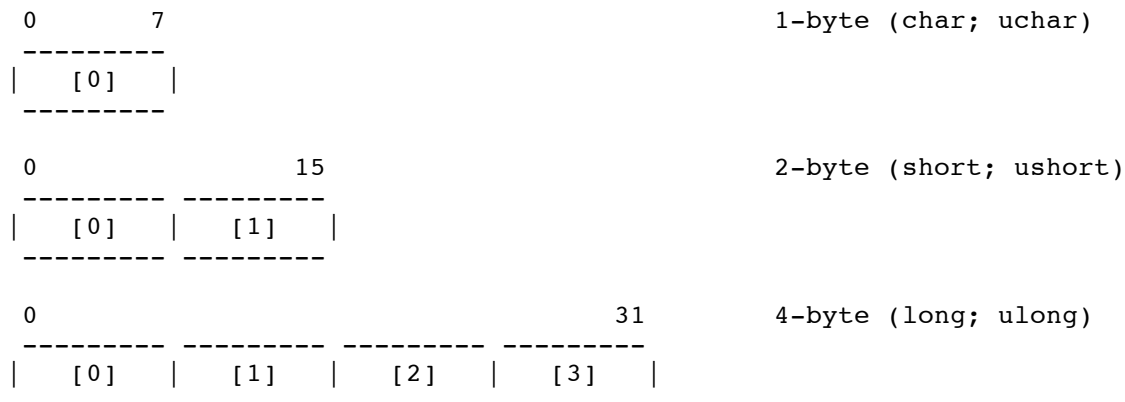
Thus,

$$S_{22} = \text{sqrt}(5/12) * (-.14001668365394E-05) = -9.038038E-07 \text{ (un-normalized)}$$

which matches closely the example given by Lambeck [11].

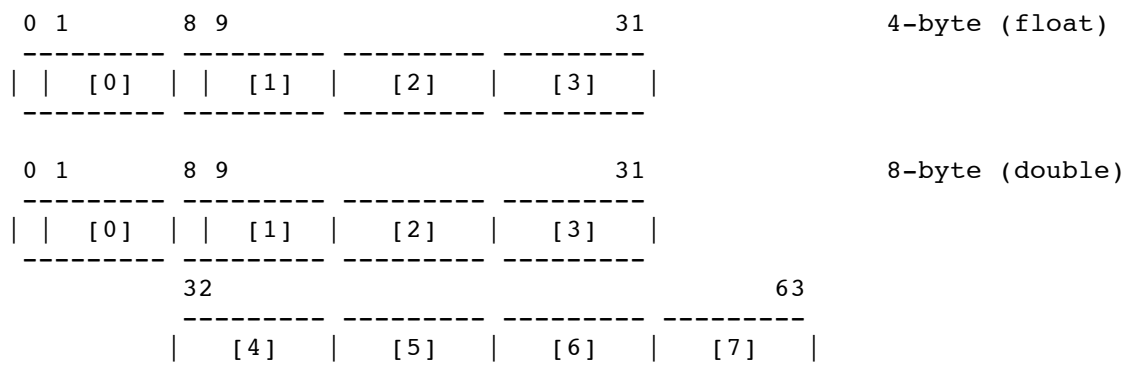
## Appendix B. BINARY DATA FORMAT

### B.1. IEEE INTEGER FIELDS



IEEE binary integers are stored in one, two, or four consecutive 8-bit bytes. Unsigned integers `uchar`, `ushort`, `ulong`, which always represent positive values, contain 8, 16, or 32 binary bits, respectively. As illustrated above, the significance increases from the rightmost bit to the leftmost (bit 0). Signed integers (`char`, `short`, `long`) are stored in the same way, except that negative values are formed by taking the corresponding positive value, complementing each bit, then adding unity -- known as "two's complement" format. As a consequence, a negative value always has bit 0 set "on". Integers are written externally in increasing byte-number order, i.e. [0], [1], etc., so that more significant bits always precede less significant ones. For example, the short value -2 is stored as a pair of bytes valued 0xff, 0xfe.

### B.2. IEEE Floating-Point Fields



IEEE single- (double-) precision floating point numbers (known to IEEE enthusiasts as E-type floating-point formats, respectively) are stored in four (eight) consecutive bytes. Bit number 0 contains a sign indicator, S. Bits 1 through 8 (11) contain a binary exponent, E. The significance increases from bit 8 (11) through bit 1. Bits 9 (12) through 31 (63) contain a mantissa M, a 23-bit (52-bit) binary fraction whose binary point lies immediately to the left of bit 9 (12). The significance increases from bit 31 (63) through bit 9 (11). The value of the single-precision field is given by

$$S \quad E-127 \\ (-1) * 2^{E-127} * (1+M)$$

The value of the double-precision field is given by

$$S \quad E-1023 \\ (-1) * 2^{E-1023} * (1+M)$$

The numbers are stored externally in increasing byte-number order, i.e. [0], [1], etc. For example, the maximum single-precision float value +3.40282347E+38 is stored as four bytes valued 0x7f, 0x7f, 0xff, 0xff.

Special single-precision float values are represented as +Infinity (0x7f800000), -Infinity (0xff800000), quiet NaN (not a number) (0xffffffff), and signaling NaN (0x7f800001).

## Appendix C. EXAMPLE DATA PRODUCTS

### APPENDIX C.1 EXAMPLE LABEL

The following lists an example SHBDR LBL file for a Mars gravity solution, GGM2BC80.SHB, prepared by Frank Lemoine of NASA GSFC.

For MESSENGER the "INSTRUMENT\_HOST\_NAME" would be listed instead of "MESSENGER" instead of "MARS RECONNAISSANCE ORBITER". The DESCRIPTION would be changed to reflect the data content of the MESSENGER gravity solutions. Other fields (e.g., PRODUCT\_RELEASE\_DATE, PRODUCT\_ID, INSTRUMENT NAME, START\_TIME, STOP\_TIME, PRODUCT\_CREATION TIME) would also be changed as appropriate.

```

PDS_VERSION_ID          = "PDS3"
FILE_NAME                = "GGM2BC80.SHB"
RECORD_TYPE              = FIXED_LENGTH
RECORD_BYTES            = 512
FILE_RECORDS             = 336254
^SHBDR_HEADER_TABLE     = ("GGM2BC80.SHB",1)
^SHBDR_NAMES_TABLE      = ("GGM2BC80.SHB",2)
^SHBDR_COEFFICIENTS_TABLE = ("GGM2BC80.SHB",105)
^SHBDR_COVARIANCE_TABLE = ("GGM2BC80.SHB",208)

INSTRUMENT_HOST_NAME    = "MARS RECONNAISSANCE ORBITER"
TARGET_NAME              = "MARS"
INSTRUMENT_NAME         = "RADIO SCIENCE SUBSYSTEM"
DATA_SET_ID              = "MRO-M-RSS-5-SDP-V1.0"
OBSERVATION_TYPE        = "GRAVITY FIELD"
PRODUCT_ID              = "GGM2BC80.SHB"
PRODUCT_RELEASE_DATE     = 2006-02-28
DESCRIPTION              = "

```

The data in this covariance matrix are stored row-wise, in upper triangular form. The error covariance contains 21506961 elements and has 336254 records. There are 6558 parameters in the GGM2BC80.SHB covariance matrix: the C and S gravity coefficients from degree 2 to 80 (inclusive) and the GM of the Mars gravity field. The data format is big endian.

This file contains coefficients and related data for a spherical harmonic model of the Mars gravity field. Input data are from radio tracking of the Mars Global Surveyor spacecraft; no Mariner 9 or Viking data are included. Coordinate system is IAU 1991 (Davies et al., Celestial Mechanics and Dynamical Astronomy, 53, 377-397, 1992).

The model was constructed from 955,115 observations, summarized in the table below. MGS data are limited to tracking from the Aerobraking Hiatus and Science Phasing Orbit (SPO) subphases of the Orbit Insertion phase of the mission and to February 1999 to February 2000 after the orbit was circularized.

Time Periods	Total	
	Arcs	Observations
-----	-----	-----
Hiatus	2	24119
SPO-1	8	31001
SPO-2	16	157972

Feb-Mar 1999	9	76813
Apr 1999 - Feb 2000	47	665210
-----	-----	-----
Total		955115

Orbit reconstruction was improved using Mars Orbiter Laser Altimeter (MOLA) data on 5 arcs between March and December 1999. Inter-arc and intra-arc crossovers at 21343 points were included in the orbit solutions.

The gravity model was derived using a Kaula type constraint:  $\sqrt{2} \cdot 13 \cdot 10^{(-5)} / L^{*2}$  (Kaula, W.M., Theory of Satellite Geodesy, Blaisdell, Waltham, MA, 1966).

The analysis and results were described by F.G. Lemoine, D.D. Rowlands, D.E. Smith, D.S. Chinn, G.A. Neumann, and M.T. Zuber at the Spring Meeting of the American Geophysical Union, May 30 - June 3, 2000, Washington. DC.

Further improvements to the model are expected as additional MGS data are incorporated.

This product is a set of two ASCII tables: a header table and a coefficients table. Definitions of the tables follow.

This Mars gravity model was produced by F.G. Lemoine under the direction of D.E. Smith of the MGS Radio Science Team.

A reference for this gravity model is as follows:

An improved solution of the gravity field of Mars (GMM-2B) from Mars Global Surveyor, F.G. Lemoine, D.E. Smith, D.D. Rowlands, M.T. Zuber, G.A. Neumann, D.S. Chinn, and D.E. Pavlis, J. Geophys. Res., 106(E10), pp. 23359-23376. October 25, 2001."

```

START_TIME           = 1997-10-13T00:00:00
STOP_TIME            = 2000-02-29T12:05:00
START_ORBIT_NUMBER   = 19
STOP_ORBIT_NUMBER    = 4375
PRODUCT_CREATION_TIME = 2000-09-18T00:00:00.000
PRODUCER_FULL_NAME   = "FRANK G. LEMOINE"
PRODUCER_INSTITUTION_NAME = "GODDARD SPACE FLIGHT CENTER"
PRODUCT_VERSION_TYPE = "FINAL"
PRODUCER_ID          = "MRO GST"
SOFTWARE_NAME        = "SOLVE.F90INLINE3;2000.01"

```

```

OBJECT                = SHBDR_HEADER_TABLE
ROWS                  = 1
COLUMNS              = 9
ROW_BYTES             = 56
INTERCHANGE_FORMAT    = BINARY
DESCRIPTION           = "The SHBDR Header includes
descriptive information about the spherical harmonic
coefficients that follow in SHBDR_COEFFICIENTS_TABLE.
The header consists of a single record of nine data
columns requiring 56 bytes. The Header is followed by
a pad of binary integer zeroes to ensure alignment
with RECORD_BYTES."

```

```

OBJECT                = COLUMN

```

```

NAME                = "REFERENCE RADIUS"
DATA_TYPE            = IEEE_REAL
START_BYTE          = 1
BYTES               = 8
UNIT                = "KILOMETER"
DESCRIPTION          = "The assumed reference
radius of the spherical planet."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
NAME                = "CONSTANT"
DATA_TYPE            = IEEE_REAL
START_BYTE          = 9
BYTES               = 8
UNIT                = "KM^3/S^2"
DESCRIPTION          = "For a gravity field model
the gravitational constant GM in km cubed per seconds
squared for the planet. For a topography model, set to 1"
END_OBJECT          = COLUMN

OBJECT              = COLUMN
NAME                = "UNCERTAINTY IN CONSTANT"
DATA_TYPE            = IEEE_REAL
START_BYTE          = 17
BYTES               = 8
UNIT                = "KM^3/S^2"
DESCRIPTION          = "For a gravity field model
the uncertainty in the gravitational constant GM in km
cubed per seconds squared for the planet. For a topography
model, set to 0."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
NAME                = "DEGREE OF FIELD"
DATA_TYPE            = MSB_INTEGER
START_BYTE          = 25
BYTES               = 4
UNIT                = "N/A"
DESCRIPTION          = "Degree of the model field."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
NAME                = "ORDER OF FIELD"
DATA_TYPE            = MSB_INTEGER
START_BYTE          = 29
BYTES               = 4
UNIT                = "N/A"
DESCRIPTION          = "Order of the model field."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
NAME                = "NORMALIZATION STATE"
DATA_TYPE            = MSB_INTEGER
START_BYTE          = 33
BYTES               = 4
UNIT                = "N/A"
DESCRIPTION          = "The normalization indicator.
For gravity field:
    0   coefficients are unnormalized
    1   coefficients are normalized

```

```

    2 other."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
  NAME               = "NUMBER OF NAMES"
  DATA_TYPE         = MSB_INTEGER
  START_BYTE         = 37
  BYTES              = 4
  UNIT               = "N/A"
  DESCRIPTION        = "Number of valid names in
the SHBDR Names Table. Also, the number of valid
coefficients in the SHBDR Coefficients Table."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
  NAME               = "REFERENCE LONGITUDE"
  POSITIVE_LONGITUDE_DIRECTION = "EAST"
  DATA_TYPE         = IEEE_REAL
  START_BYTE         = 41
  BYTES              = 8
  UNIT               = "DEGREE"
  DESCRIPTION        = "The reference longitude for
the spherical harmonic expansion; normally 0."
END_OBJECT          = COLUMN

OBJECT              = COLUMN
  NAME               = "REFERENCE LATITUDE"
  DATA_TYPE         = IEEE_REAL
  START_BYTE         = 49
  BYTES              = 8
  UNIT               = "DEGREE"
  DESCRIPTION        = "The reference latitude for
the spherical harmonic expansion; normally 0."
END_OBJECT          = COLUMN

END_OBJECT          = SHBDR_HEADER_TABLE

OBJECT              = SHBDR_NAMES_TABLE
  ROWS               = 6558
  COLUMNS           = 1
  ROW_BYTES          = 8
  INTERCHANGE_FORMAT = BINARY
  DESCRIPTION        = "The SHBDR Names Table
contains names for the solution parameters (including
gravity field coefficients) which will follow in
SHBDR_COEFFICIENTS_TABLE. The order of the names
in SHBDR_NAMES_TABLE corresponds identically to the
order of the parameters in SHBDR_COEFFICIENTS_TABLE.
Each coefficient name is of the form Cij or Sij
where i is the degree of the coefficient and j is
the order of the coefficient. Both indices are three-
digit zero-filled right-justified ASCII character strings
(for example, C010005 for the 10th degree 5th order C
coefficient, or S002001 for the 2nd degree 1st order
S coefficient). The eighth byte in the table is an
ASCII blank used to ensure that the row length
is equal to RECORD_BYTES. Names of other solution
parameters are limited to 8 ASCII characters; if less
than 8, they will be left-justified and padded with
ASCII blanks. The Names Table itself will be padded

```



with ASCII blanks, if necessary, so that its length is an integral multiple of RECORD\_BYTES."

```
OBJECT                = COLUMN
  NAME                 = "PARAMETER NAME"
  DATA_TYPE           = CHARACTER
  START_BYTE           = 1
  BYTES                = 8
  UNIT                 = "N/A"
  DESCRIPTION           = "The name of the
  coefficient or other solution parameter, left-
  justified and padded with ASCII blanks (if needed)
  to 8 characters."
END_OBJECT            = COLUMN

END_OBJECT            = SHBDR_NAMES_TABLE

OBJECT                = SHBDR_COEFFICIENTS_TABLE
  ROWS                 = 6558
  COLUMNS             = 1
  ROW_BYTES            = 8
  INTERCHANGE_FORMAT   = BINARY
  DESCRIPTION           = "The SHBDR Coefficients Table
  contains the coefficients and other solution parameters
  for the spherical harmonic model. The order of the
  coefficients in this table corresponds exactly to the
  order of the coefficient and parameter names in
  SHBDR_NAMES_TABLE. The SHBDR Coefficients Table will be
  padded with double precision DATA_TYPE zeroes so that
  its total length is an integral multiple of RECORD_BYTES."

OBJECT                = COLUMN
  NAME                 = "COEFFICIENT VALUE"
  DATA_TYPE           = IEEE_REAL
  START_BYTE           = 1
  BYTES                = 8
  UNIT                 = "N/A"
  DESCRIPTION           = "A coefficient Cij or
  Sij or other solution parameter as specified in the
  SHBDR Names Table."
END_OBJECT            = COLUMN

END_OBJECT            = SHBDR_COEFFICIENTS_TABLE

OBJECT                = SHBDR_COVARIANCE_TABLE
  ROWS                 = 21506961
  COLUMNS             = 1
  ROW_BYTES            = 8
  INTERCHANGE_FORMAT   = BINARY
  DESCRIPTION           = "The SHBDR Covariance Table
  contains the covariances for the spherical harmonic model
  coefficients and other solution parameters. The order of
  the covariances in this table is defined by the product
  of the SHBDR Names Table with its transpose, except that
  redundant terms are omitted on their second occurrence.
  The SHBDR Covariance Table will be padded with double
  precision DATA_TYPE zeroes so that its total length is
  an integral multiple of RECORD_BYTES."

OBJECT                = COLUMN
```

```

NAME                = "COVARIANCE VALUE"
DATA_TYPE           = IEEE_REAL
START_BYTE         = 1
BYTES              = 8
UNIT               = "N/A"
DESCRIPTION        = "The covariance value
for the coefficients and other solution parameters
specified by the product of SHBDR_NAMES_TABLE with
its transpose, after omitting redundant terms."
END_OBJECT         = COLUMN

```

```
END_OBJECT          = SHBDR_COVARIANCE_TABLE
```

```
END
```

## APPENDIX C.2 EXAMPLE SHBDR DATA OBJECT OUTPUT

The following lists the first few lines from an example SHBDR file, the GGM2BC80.SHB Gravity field solution covariance.

We describe below the extracts from a FORTRAN program to read the above GGM2BC280.SHB covariance file, the error covariance of the gravity solution GMM2B.

The SHB file is opened with the following FORTRAN open statement. The key is that the SHB file is a direct access binary file with a record length (in this example) of 512 bytes.

i.e.

```
open (10, file='ggm2bc80.shb', status='old', access='DIRECT', RECL=512)
```

The first record reads the general solution information, where the variables have been carefully predefined at the top of the program.

```

.....
real*8 ae, gm, gmsig, reflon, reflat
integer*4 lmax,mmax,inorm, nvar
read(10,rec=1)ae, gm, gmsig, lmax, mmax, inorm, nvar, reflon, reflat
.....

```

On output these records are:

```

ae      = 3397.0
gm      = 42828.371901      | GM in km**3/sec**2
gmsig   = 7.40E-05         | GM sigma in km**3/sec**2
lmax    = 80
mmax    = 80
inorm   = 1
nvar    = 6558              | total number of parameters in the solution.
reflon  = 0.0E+0
reflat  = 0.0E+0

```

The next step is to read the coefficient name table and compute the number of lines in the coefficient name table. In this example file there are 64 8 byte characters per record of 512 bytes.

```

.....
nline = (nvar/64) + 1
.....
c integer multiplication on the following line is intentional
c we need to know number of variables on the last line
.....
jend = nvar - (nvar/64)*64
.....

```

Record 2, or the first record of the names table contains the following:

C002000	C002001	C002002	C003000	C003001	C003002	C003003	C004000
C004001	C004002	C004003	C004004	C005000	C005001	C005002	C005003
C005004	C005005	C006000	C006001	C006002	C006003	C006004	C006005
C006006	C007000	C007001	C007002	C007003	C007004	C007005	C007006
C007007	C008000	C008001	C008002	C008003	C008004	C008005	C008006
C008007	C008008	C009000	C009001	C009002	C009003	C009004	C009005
C009006	C009007	C009008	C009009	C010000	C010001	C010002	C010003
C010004	C010005	C010006	C010007	C010008	C010009	C010010	C011000

Record 104 contains the last few coefficient names of the solution+GM:

S080052	S080053	S080054	S080055	S080056	S080057	S080058	S080059
S080060	S080061	S080062	S080063	S080064	S080065	S080066	S080067
S080068	S080069	S080070	S080071	S080072	S080073	S080074	S080075
S080076	S080077	S080078	S080079	S080080	GM		

The Coefficients table begins at Record 105:  
The first eight variables of that record are:

-0.87451D-03	0.13938D-09	-0.84178D-04	-0.11887D-04	0.39053D-05
-0.15863D-04	0.35339D-04	0.51258D-05		

The first coefficient value is for C20.

The Coefficients table ends at Record 207 with 30 valid records and the remainder zero filled:

-0.39660D-07	0.25145D-08	0.27213D-07	0.60636D-07	0.25307D-07
0.40813D-08	0.16849D-07	0.16050D-07		
-0.30849D-07	-0.26461D-07	-0.79262D-08	0.35247D-07	0.53467D-08
0.33029D-07	0.35339D-07	0.28539D-07		
-0.30311D-10	0.38384D-07	-0.19836D-07	0.75625D-07	-0.19420D-07
0.34309D-09	-0.17577D-07	0.36022D-07		
0.42967D-07	0.42482D-07	-0.40326D-07	-0.19721D-07	-0.53860D-07
0.42828D+14				
.....				

The last valid record is the value of GM for this solution, as per the order specified in the names record.